

Completing the Square

Solve each equation by completing the square.

1. $x^2 - 2x = 15$

2. $x^2 + 6x = 14$

3. $x^2 - 8x = -5$

4. $x^2 - 10x - 3 = 0$

5. $x^2 + 4x = -1$

6. $x^2 - 20x + 2 = 0$

Completing the Square

Solve each equation by completing the square.

1. $x^2 - 2x = 15$

$$x^2 - 2x + \left(\frac{2}{2}\right)^2 = 15 + \left(\frac{2}{2}\right)^2$$

$$x^2 - 2x + 1 = 15 + 1$$

$$(x-1)^2 = 16$$

$$x-1 = \pm 4$$

$$x = 5 \text{ or } -3$$

2. $x^2 + 6x = 14$

$$x^2 + 6x + \left(\frac{6}{2}\right)^2 = 14 + \left(\frac{6}{2}\right)^2$$

$$x^2 + 6x + 9 = 14 + 9$$

$$(x+3)^2 = 23$$

$$x = \pm\sqrt{23} - 3$$

3. $x^2 - 8x = -5$

$$x^2 - 8x + 16 = -5 + 16$$

$$(x-4)^2 = 11$$

$$x = \pm\sqrt{11} + 4$$

4. $x^2 - 10x - 3 = 0$

$$x^2 - 10x + 25 = 3 + 25$$

$$(x-5)^2 = 28$$

$$x = \pm\sqrt{28} + 5$$

5. $x^2 + 4x = -1$

$$x^2 + 4x + 4 = -1 + 4$$

$$(x+2)^2 = 3$$

$$x = \pm\sqrt{3} - 2$$

6. $x^2 - 20x + 2 = 0$

$$x^2 - 20x + 100 = -2 + 100$$

$$(x-10)^2 = 98$$

$$x = \pm\sqrt{98} + 10$$