1. The sum of two consecutive odd numbers is 156. What are the numbers?

2. If n represents an odd integer, write expressions in terms of n that represent the next three consecutive odd integers. If the four consecutive odd integers have a sum of 56, find the numbers.

1. The sum of two consecutive odd numbers is 156. What are the numbers?

If we let n represent one odd number, then n + 2 represents the next consecutive odd number.

$$n + (n + 2) = 156$$

$$2n + 2 - 2 = 156 - 2$$

$$2n = 154$$

$$\left(\frac{1}{2}\right)(2n) = \left(\frac{1}{2}\right)(154)$$

$$n = 77$$

The two numbers are 77 and 79.

2. If n represents an odd integer, write expressions in terms of n that represent the next three consecutive odd integers. If the four consecutive odd integers have a sum of 56, find the numbers.

If we let n represent an odd integer, then n + 2, n + 4, and n + 6 represent the next three consecutive odd integers.

$$n + (n + 2) + (n + 4) + (n + 6) = 56$$

$$4n + 12 = 56$$

$$4n + 12 - 12 = 56 - 12$$

$$4n = 44$$

$$n = 11$$

The numbers are 11, 13, 15, and 17.

3. Six times the sum of three consecutive odd integers is -18. Find the integers.

4. The sum of two consecutive even numbers is 54. Find the numbers.

3. Six times the sum of three consecutive odd integers is -18. Find the integers.

If we let n represent the first odd integer, then n+2 and n+4 represent the next two consecutive odd integers.

$$6(n + (n + 2) + (n + 4)) = -18$$

$$6(3n + 6) = -18$$

$$18n + 36 = -18$$

$$18n + 36 - 36 = -18 - 36$$

$$18n = -54$$

$$n = -3$$

$$n + 2 = -1$$

$$n + 4 = 1$$

The integers are -3, -1, and 1.

4. The sum of two consecutive even numbers is 54. Find the numbers.

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First consecutive even integer: x
Second consecutive even integer: x + 2
x + (x + 2) = 542x + 2 = 542x + 2 - 2 = 54 - 22x + 0 = 52\left(\frac{1}{2}\right)(2x) = \left(\frac{1}{2}\right)(52)x = 26
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The consecutive even integers are 26 and 28.

5. I am thinking of a number. If you multiply my number by 4, add -4 to the product, and then take $\frac{1}{3}$ of the sum, the result is -6. Find my number.

6. A number is $\frac{1}{7}$ of another number. The difference of the numbers is 18. (Assume that you are subtracting the smaller number from the larger number.) Find the numbers.

5. I am thinking of a number. If you multiply my number by 4, add -4 to the product, and then take $\frac{1}{3}$ of the sum, the result is -6. Find my number.

Let n represent the given number.

$$\frac{1}{3}(4n + (-4)) = -6$$
$$\frac{4}{3}n - \frac{4}{3} = -6$$
$$\frac{4}{3}n - \frac{4}{3} + \frac{4}{3} = -6 + \frac{4}{3}$$
$$\frac{4}{3}n = \frac{-14}{3}$$
$$n = -3\frac{1}{2}$$

6. A number is $\frac{1}{7}$ of another number. The difference of the numbers is 18. (Assume that you are subtracting the smaller number from the larger number.) Find the numbers.

If we let n represent a number, then $\frac{1}{7}n$ represents the other number.

$$n - \left(\frac{1}{7}n\right) = 18$$
$$\frac{7}{7}n - \frac{1}{7}n = 18$$
$$\frac{6}{7}n = 18$$
$$\frac{7}{6} \cdot \frac{6}{7}n = \frac{7}{6} \cdot 18$$
$$1n = 7 \cdot 3$$
$$n = 21$$

The numbers are 21 and 3.

7. A number is 6 greater than $\frac{1}{2}$ another number. If the sum of the numbers is 21, find the numbers.

7. A number is 6 greater than $\frac{1}{2}$ another number. If the sum of the numbers is 21, find the numbers.

If we let n represent a number, then $rac{1}{2}n+6$ represents the first number.

$$n + \left(\frac{1}{2}n + 6\right) = 21$$
$$\left(n + \frac{1}{2}n\right) + 6 = 21$$
$$\left(\frac{2}{2}n + \frac{1}{2}n\right) + 6 = 21$$
$$\frac{3}{2}n + 6 = 21$$
$$\frac{3}{2}n + 6 - 6 = 21 - 6$$
$$\frac{3}{2}n + 0 = 15$$
$$\frac{3}{2}n + 0 = 15$$
$$\frac{3}{2}n = 15$$
$$\frac{3}{2}n = 15$$
$$\frac{2}{3} \cdot \frac{3}{2}n = \frac{2}{3} \cdot 15$$
$$1n = 2 \cdot 5$$
$$n = 10$$

Since the numbers sum to 21, they are 10 and 11.