

Student Outcomes

- Students use the known formula for the volume of a right rectangular prism (length \times width \times height). •
- Students understand the volume of a right prism to be the area of the base times the height.
- Students compute volumes of right prisms involving fractional values for length.

Related Topics: More Lesson Plans for Grade 7 Common Core Math

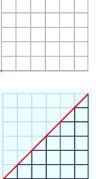
Lesson Notes

Students extend their knowledge of obtaining volumes of right rectangular prisms via dimensional measurements to understand how to calculate the volumes of other right prisms. This concept will later be extended to finding the volumes of liquids in right prism shaped containers then extended again (in Module 6) to finding the volumes of irregular solids using displacement of liquids in containers. The problem set scaffolds in the use of equations to calculate unknown dimensions.

Classwork

Opening Exercise (5 minutes)

Opening Exercise	
The volume of a solid is a quantity given by the number of unit cubes needed to fill the solid. Mos baseballs, people—cannot be filled with unit cubes or assembled from cubes. Yet such solids still I Fortunately, we do not need to assemble solids from unit cubes in order to calculate their volume. interesting examples of a solid that cannot be assembled from cubes but whose volume can still be calculated from a formula is a right triangular prism.	have volume.
What is the area of the square pictured on the right? Explain.	
The area of the square is 36 units ² because the region is filled with 36 square regions that are 1 unit by 1 unit, or 1 unit ² .	
Draw the diagonal joining the two given points then darken the grid lines within the lower triangular region. What is area of that triangular region? Explain.	A
The area of the triangular region is 18 units ² . There are 15 unit squares from the original square and 6 triangular regions that are $\frac{1}{2}$ unit ² . The 6 triangles can be paired together to form 3 units ² . Altogether the area of the triangular region is (15 + 3) units ² = 18 units ² .	



- How do the areas of the square and the triangular region compare?
 - The area of the triangular region is half the area of the square region.



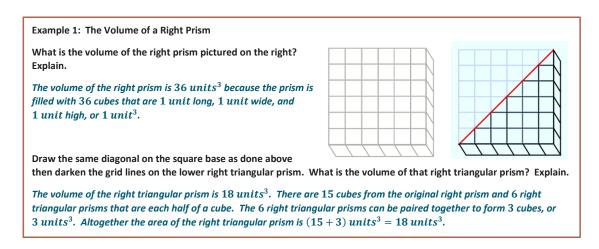
The Volume of a Right Prism 3/19/14





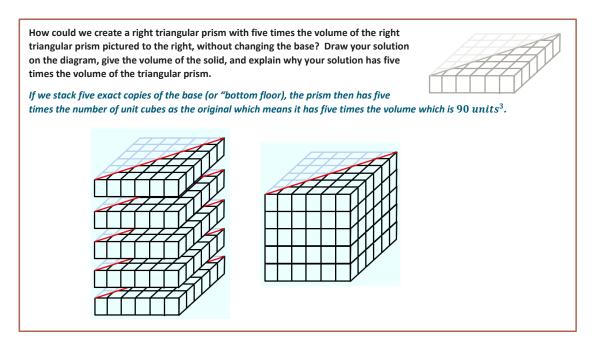
Example 1 (15 minutes): The Volume of a Right Prism

Example 1 is a continuation of the Opening Exercise.



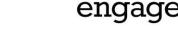
- In both cases, slicing the square (or square face) along its diagonal divided the area of the square into two equal size triangular regions. When we sliced the right prism, however, what remained constant?
 - The height of the given right rectangular prism and the resulting triangular prism are unchanged at 1 unit.

The argument used here is true in general for all right prisms. Since polygonal regions can be decomposed into triangles and rectangles, it is true that the polygonal base of a given right prism can be decomposed into triangular and rectangular regions that are bases of a set of right prisms that have heights equal to the height of the given right prism.



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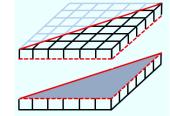
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What could we do to cut the volume of the right triangular prism pictured on the right in half without changing the base? Draw your solution on the diagram, give the volume of the solid, and explain why your solution has half the volume of the given triangular prism. If we slice the height of the prism in half, each of the unit cubes that make up the triangular prism will have half the volume as in the original right triangular prism. The volume of the new right triangular prism is 9 $units^3$.



- What can we conclude about how to find the volume of any right prism?
 - The volume of any right prism can be found by multiplying the area of its base times the height of the prism.
 - If we let V represent the volume of a given right prism, let B represent the area of the base of that given right prism, and let h represent the height of that given right prism, then:

V = Bh

Have students complete the sentence below in their student materials.

Scaffolding:

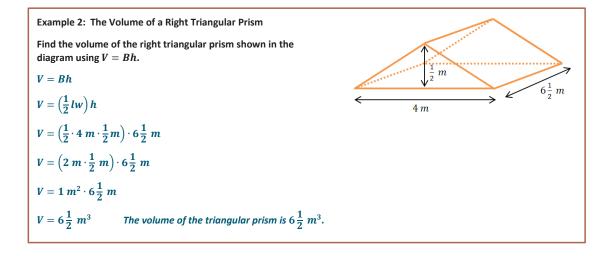
Students often form the misconception that changing the dimensions of a given right prism will affect the prism's volume by the same factor. Use this exercise to show that the volume of the cube was cut in half because the height was cut in half. If all dimensions of a unit cube were cut in half, the resulting volume would be $\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{8}$ which of course is not equal to $\frac{1}{2}$ unit³.

To find the volume (V) of any right prism...

Multiply the area of the right prism's base (B) times the height of the right prism (h), V = Bh.

Example 2 (5 minutes): The Volume of a Right Triangular Prism

Students calculate the volume of a triangular prism that has not been decomposed from a rectangle.





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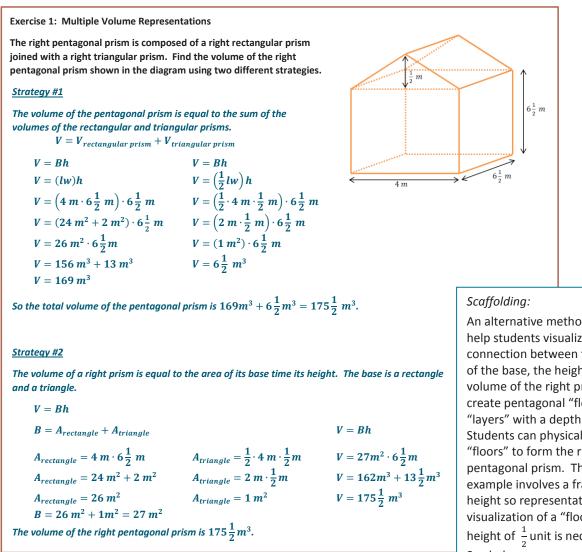
The Volume of a Right Prism 3/19/14



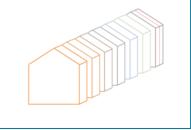
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Exercise 1 (10 minutes): Multiple Volume Representations

Students find the volume of the right pentagonal prism using two different strategies.



An alternative method that will help students visualize the connection between the area of the base, the height, and the volume of the right prism is to create pentagonal "floors" or "layers" with a depth of 1 unit. Students can physically pile the "floors" to form the right pentagonal prism. This example involves a fractional height so representation or visualization of a "floor" with a height of $\frac{1}{2}$ unit is necessary. See below:



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Closing (2 minutes)

- What are some strategies that we can use to find the volume of three-dimensional objects?
 - Find the area of the base, then multiply times the prism's height; decompose the prism into two or more smaller prisms of the same height and add the volumes of those smaller prisms.
- The volume of a solid is always greater than or equal to zero.
- If two solids are identical, they have equal volumes.
- If a solid *S* is the union of two non-overlapping solids *A* and *B*, then the volume of solid *S* is equal to the sum of the volumes of solids *A* and *B*.

Exit Ticket (8 minutes)



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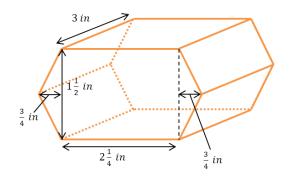


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Lesson 23: The Volume of a Right Prism

Exit Ticket

The base of the right prism is a hexagon composed of a rectangle and two triangles. Find the volume of the right hexagonal prism using the formula V = Bh.





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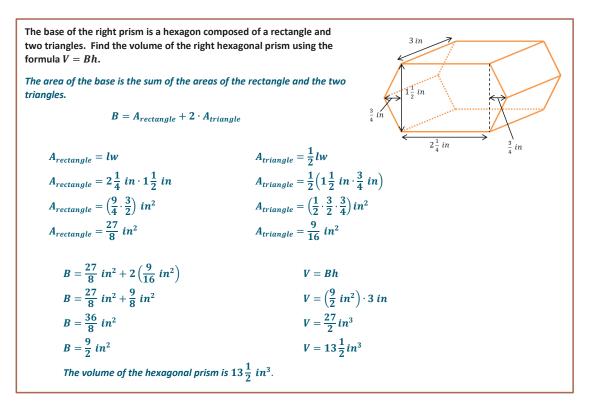




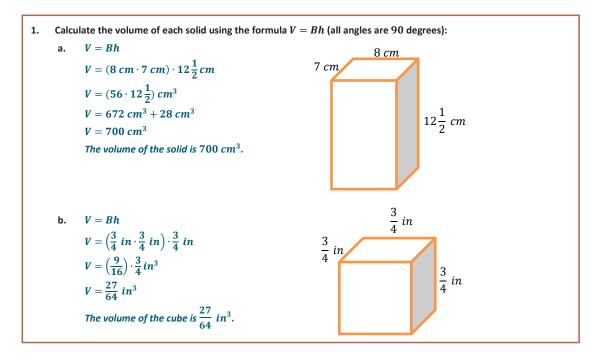
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Exit Ticket Sample Solutions



Problem Set Sample Solutions

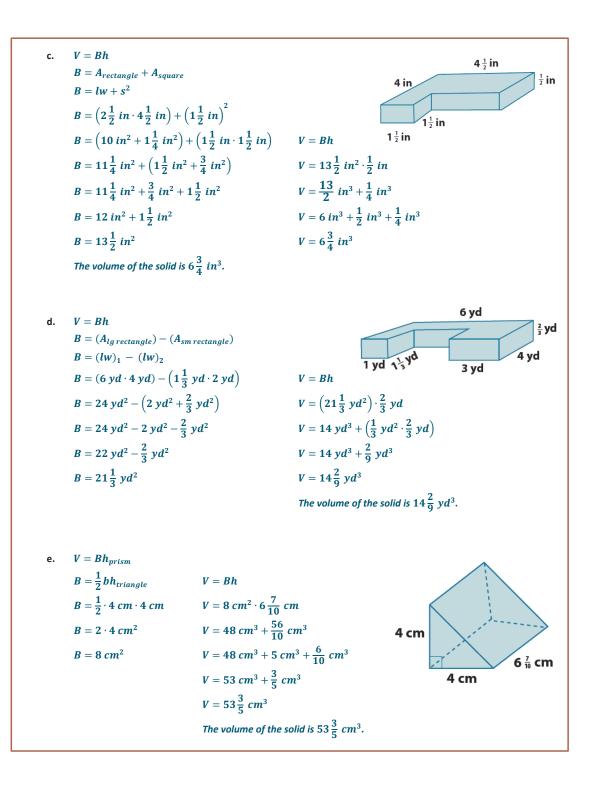




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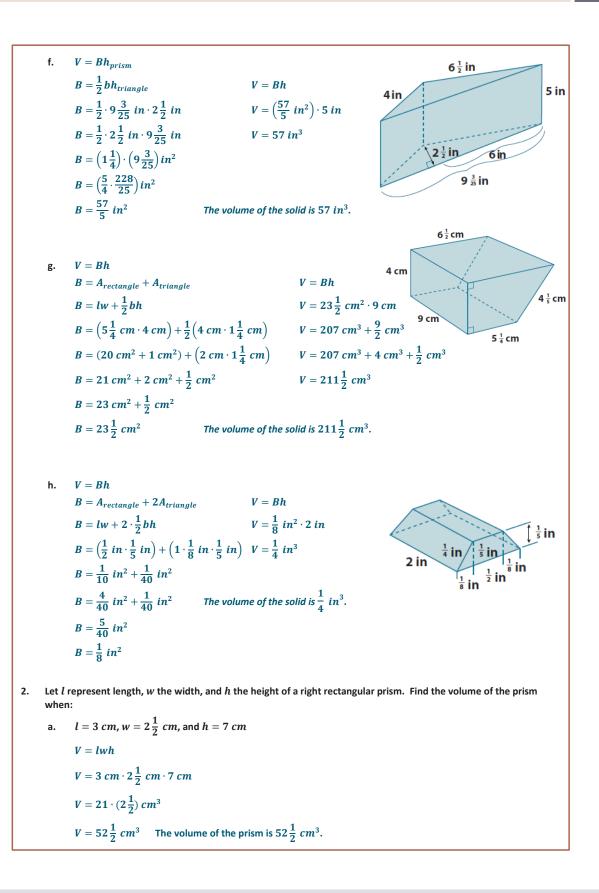
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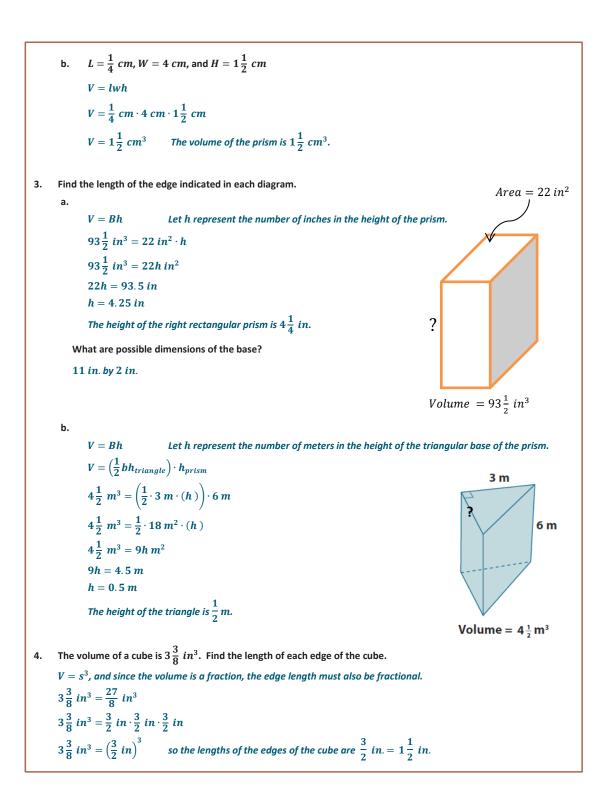
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5. Given a right rectangular prism with a volume of $7\frac{1}{2}ft^3$, a length of 5 ft, and a width of 2 ft, find the height of the prism. V = Bh V = (lw)h Let h represent the number of feet in the height of the prism. $7\frac{1}{2}ft^3 = (5ft \cdot 2ft) \cdot h$ $7\frac{1}{2}ft^3 = 10 ft^2 \cdot h$ $7.5 ft^3 = 10h ft^2$ h = 0.75 ftThe height of the right rectangular prism is $\frac{3}{4}ft$ (or 9 inches).



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