

Student Outcomes

Students find the areas of triangles and simple polygonal regions in the coordinate plane with vertices at grid points by composing into rectangles and decomposing into triangles and quadrilaterals.

Related Topics: More Lesson Plans for Grade 7 Common Core Math

Lesson Notes

Students will extend their knowledge of finding area to figures on a coordinate plane. The lesson begins with a proof of the area of a parallelogram. In Grade 6, students proved the area of a parallelogram through a different approach. This lesson will draw heavily on MP.7 (look for and make use of structure). Students will notice and take advantage of figures composed of simpler ones to determine area.

Classwork

Example 1 (20 minutes): Area of a Parallelogram

Allow students to work through parts (a)–(e) of the example either independently or in groups. Circulate the room to check student progress and to ensure that students are drawing the figures correctly. Debrief before having them move on to part (f).

Example: Area of a Parallelogram The coordinate plane below contains figure *P*, parallelogram *ABCD*. а. Write the ordered pairs of each of the vertices next to the vertex points. $\vec{P}(0,2)$ See figure. S b. Draw a rectangle surrounding figure P that has vertex points of A Ρ and C. Label the two triangles in the figure as S and T. See figure. (-3 (2 Find the area of the rectangle. c. Base = 8 units Height = 6 unitsArea = 8 units \times 6 units = 48 sq. units



Lesson 19: Date:

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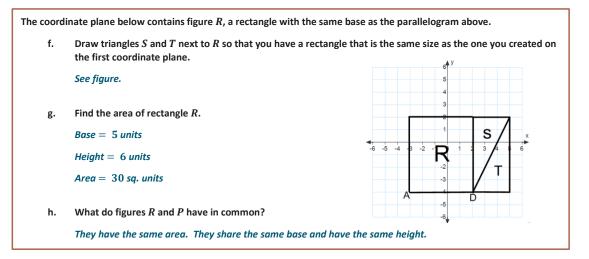


Find the area of each triangle.	
Figure S	Figure T
Base = 3 units	Base = 3 units
Height = 6 units	Height = 6 units
$Area = \frac{1}{2} \times 3 \text{ units} \times 6 \text{ units}$	$Area = \frac{1}{2} \times 3 \text{ units} \times 6 \text{ units}$
= 9 sq. units	= 9 sq. units
e. Use these areas to find the area of parallelogram <i>ABCD</i> .	
Area $P = Area$ of rectangle – Area $S - Area T$	
= 48 sq. units -9 sq. units -9 sq units $= 30$ sq. units	
	Figure S Base = 3 units Height = 6 units Area = $\frac{1}{2} \times 3$ units × 6 units = 9 sq. units Use these areas to find the area of particular definition of the area of the

Stop students here and discuss responses.

- How did you find the base and height of each figure?
 - By using the scale on the coordinate plane.
- How did you find the area of the parallelogram?
 - By subtracting the areas of the triangles from the area of the rectangle.

Assist students with part (f) if necessary and then give them time to finish the exploration.



Debrief and allow students to share responses. Draw the height of the parallelogram to illustrate that it has the same height as rectangle R.

- Since the larger rectangles are the same size, their areas must be equal. Write this on the board: Area of P + Area of S + Area of T = Area of R + Area of S + Area of T
- Based on the equation, what must be true about the area of *P*?
 - Area of P = Area of R
- How can we find the area of a parallelogram?
 - Area of Parallelogram = Base × Height



Lesson 19: Date:

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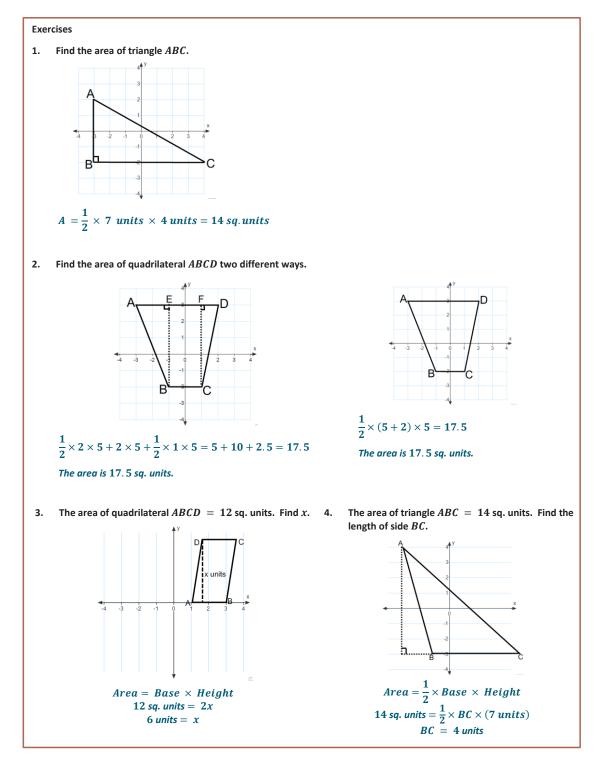
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Exercises (17 minutes)

Have students work on the exercises independently and then check answers with a partner. Then, discuss results as a class.

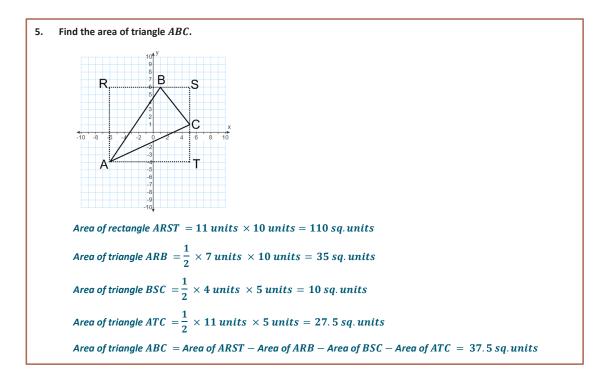


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- What shape is the quadrilateral in Exercise 2?
 - Trapezoid.
- What methods did you use to find the area?
 - ^a Splitting the figure into two right triangles and a rectangle or using the area formula for a trapezoid.
- Which method was easier for finding the area?
 - Answers will vary.
- For Exercise 4, what piece of information was missing? Why couldn't we find it using the coordinate plane?
 - The base was missing. We could measure the height but not the base because no scale was given on the *x*-axis.
- For Exercise 5, why couldn't we find the area of triangle ABC by simply using its base and height?
 - Because of the way the triangle was oriented, we could not measure the exact length of the base or the height using the coordinate plane.

Closing (3 minutes)

Review relevant vocabulary and formulas from this lesson. These terms and formulas should be a review from earlier grades and previous lessons in this module.

Vocabulary:

MP.7

quadrilateral

rectangle

semicircle

square

parallelogram

diameter of a circle

trapezoid altitude and base of a triangle



Lesson 19: Un Date: 3/2

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Lesson 19



Area formulas:

Area of parallelogram = $Base \times Height$

Area of rectangle = Base \times Height

Area of a triangle $=\frac{1}{2} \times Base \times Height$

Area of a trapezoid = $\frac{1}{2}$ × (Base 1 + Base 2) × Height

Area of a circle = $\pi \times r^2$

- Why is it useful to have a figure on a coordinate plane?
 - The scale can be used to measure the base and height.
- What are some methods for finding the area of a quadrilateral?
 - Use a known area formula, deconstruct the figure into shapes with known area formulas, make the figure a part of a larger shape and then subtract areas.

Exit Ticket (5 minutes)







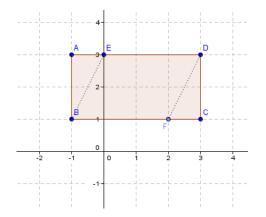
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Exit Ticket

The figure *ABCD* is a rectangle. AB = 2 units, AD = 4 units, and AE = FC = 1 unit.



1. Find the area of rectangle *ABCD*.

2. Find the area of triangle *ABE*.

- 3. Find the area of triangle *DCF*.
- 4. Find the area of the parallelogram *BEDF* two different ways.



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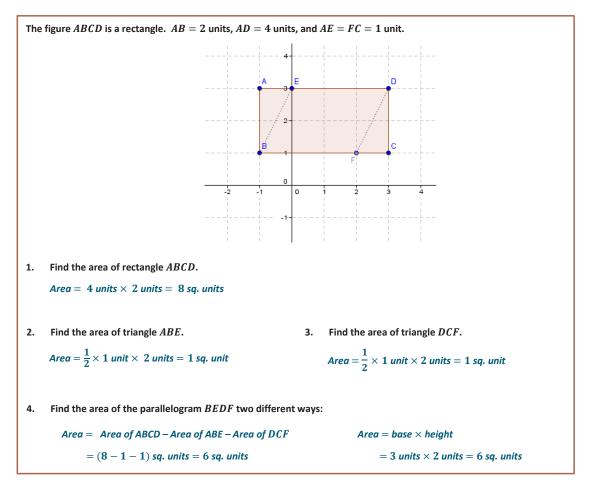
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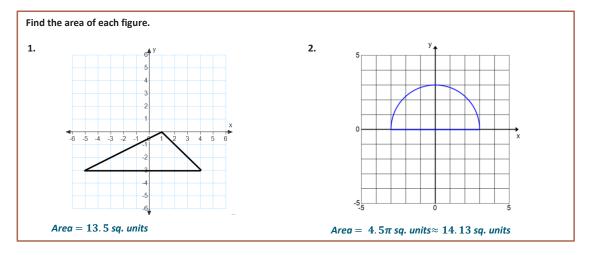




Exit Ticket Sample Solutions



Problem Set Sample Solutions

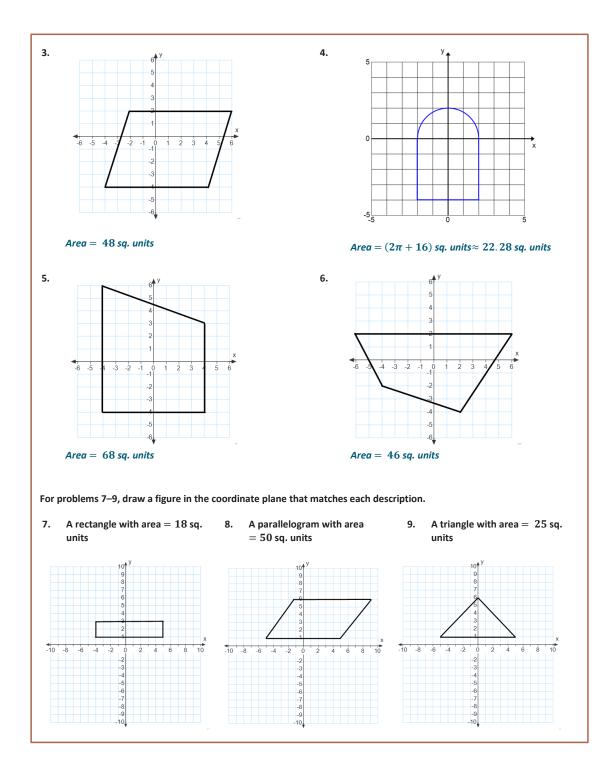




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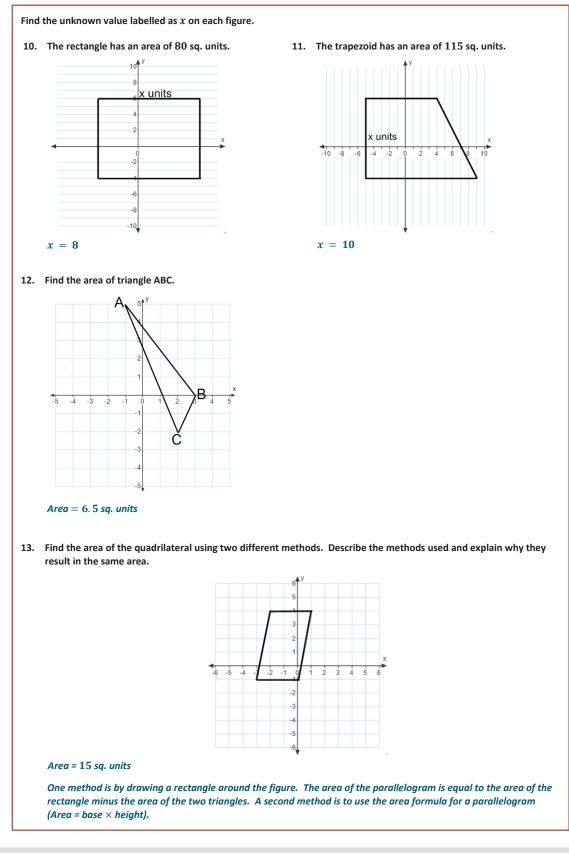
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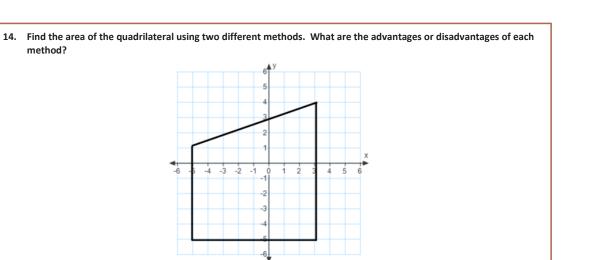
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Area = 60 sq. units

One method is to use the area formula for a trapezoid, $A = \frac{1}{2}(base 1 + base 2) \times height$. The second method is to split the figure into a rectangle and a triangle. The second method required more calculations. The first method required first recognizing the figure as a trapezoid and recalling the formula for the area of a trapezoid.



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