

Student Outcomes

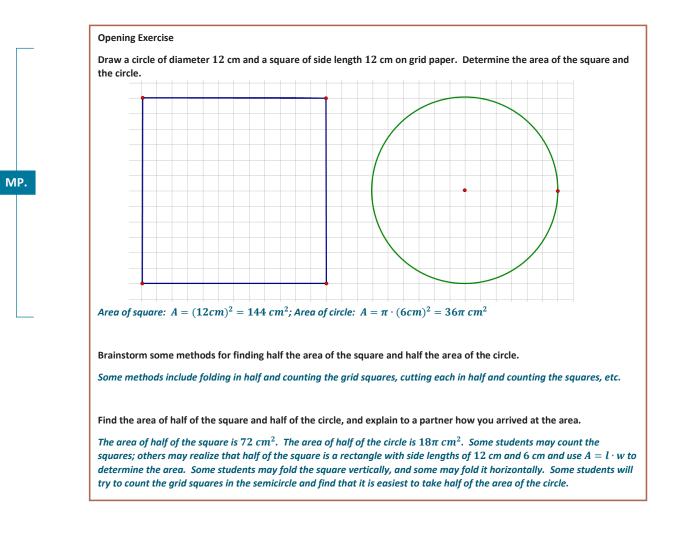
- Students examine the meaning of *quarter circle* and *semicircle*.
- Students solve area and perimeter problems for regions made out of rectangles, quarter circles, semicircles, and circles, including solving for unknown lengths when the area or perimeter is given.

Related Topics: More Lesson Plans for Grade 7 Common Core Math

Classwork

Opening Exercise (5 minutes)

Students use prior knowledge to find the area of circles, semicircles, and quarter circles and compare their areas to areas of squares and rectangles.





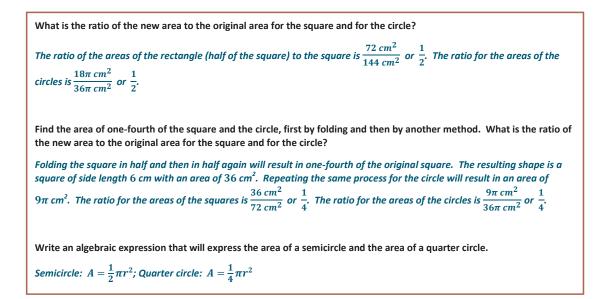
Lesson 18: Date: More Problems on Area and Circumference 3/19/14



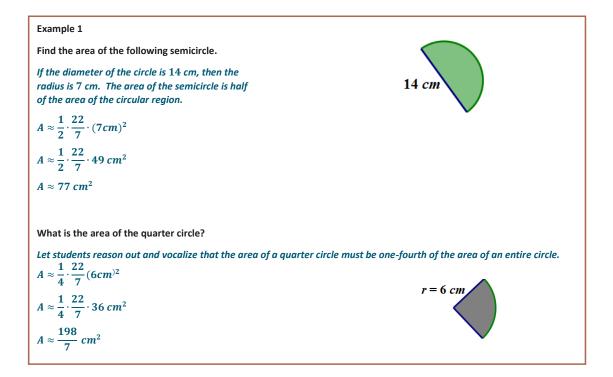
257



This work is licensed under a <u>Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License.</u>



Example 1 (8 minutes)





Lesson 18: Date: More Problems on Area and Circumference 3/19/14

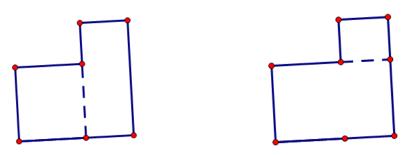






Discussion

Students should recognize that composition area problems involve the decomposition of the shapes that make up the entire region. It is also very important for students to understand that there are several perspectives in decomposing each shape and that there is not just one correct method. There is often more than one "correct" method; therefore, a student may feel that his/her solution (which looks different than the one other students present) is incorrect. Alleviate that anxiety by showing multiple correct solutions. For example, cut an irregular shape into squares and rectangles as seen below.

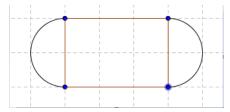


Example 2 (8 minutes)

Example 2

Marjorie is designing a new set of placemats for her dining room table. She sketched a drawing of the placement on graph paper. The diagram represents the area of the placemat consisting of a rectangle and two semicircles at either end. Each square on the grid measures 4 inches in length.

Find the area of the entire placemat. Explain your thinking regarding the solution to this problem.



The length of one side of the rectangular section is 12 inches in length, while the shorter side is 8 inches in width. The radius of the semicircular region is 4 inches. The area of the rectangular part is $(8 \text{ in}) \cdot (12 \text{ in}) = 96 \text{ in}^2$. The total area must include the two semicircles on either end of the placemat. The area of the two semi-circular regions is the same as the area of one circle with the same radius. The area of the circular region is $A = \pi \cdot (4 \text{ in})^2 = 16\pi \text{ in}^2$. In this problem, using $\pi \approx 3.14$ will make more sense because there are no fractions in the problem. The area of the semicircular regions is approximately 50.24 in^2 . The total area for the placemat is the sum of the areas of the rectangular region and the two semicircular regions, which is approximately $(96 + 50.24) \text{ in}^2 = 146.24 \text{ in}^2$.

Common Mistake: Ask students to determine how a student would solve this problem and arrive at an incorrect solution of 196.48 in². A student would arrive at this answer by including the area of the circle twice instead of once (50.24 + 50.24 + 96).

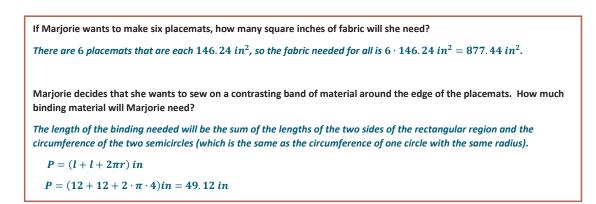


Lesson 18: Date: More Problems on Area and Circumference 3/19/14

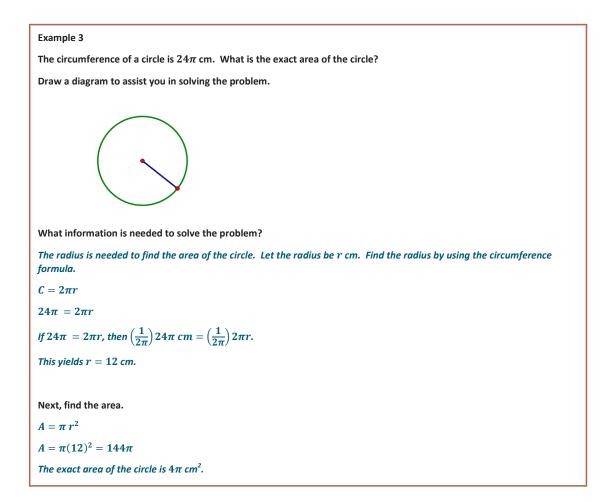








Example 3 (4 minutes)





Lesson 18: Date: More Problems on Area and Circumference 3/19/14







Exercises (10 minutes)

Students should solve these problems individually at first and then share with their cooperative groups after every other problem.

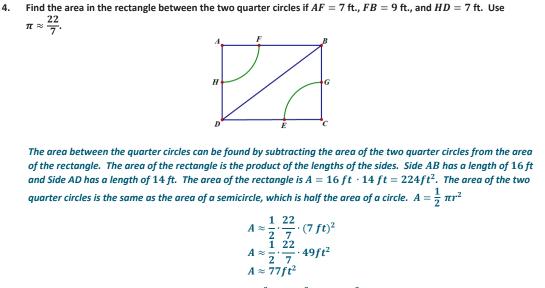
Exercises			
1.	Find the area of a circle with a diameter of 42 cm. Use $\pi pprox rac{22}{7}$.		
	If the diameter of the circle is 42 cm, then the radius is 21 cm.		
		$A = \pi r^2$	
		$A \approx \frac{22}{7} (21 \ cm)^2$	
		$A \approx 1386 \ cm^2$	
2	2. The circumference of a circle is 9π cm.		
2.	a.	What is the diameter?	
		If $C = \pi d$, then 9π cm= πd .	
		Solving the equation ford, $\frac{1}{\pi} \cdot 9\pi$ cm $= \frac{1}{\pi}\pi \cdot d$.	
		So, $9 \ cm = d$.	
	b.	What is the radius?	
		9	
		If the diameter is 9 cm, then the radius is half of that or $\frac{1}{2}$ cm.	
	c.	What is the area?	
	с.		
		The area of the circle is $A = \pi \cdot \left(\frac{9}{2} cm\right)^2$, so $= \frac{81}{4} \pi cm^2$.	
3.	If students only know the radius of a circle, what other measures could they determine? Explain how students would use the radius to find the other parts.		
	If students know the radius, then they can find the diameter. The diameter is twice as long as the radius. The circumference can be found by doubling the radius and multiplying the result by π . The area can be found by multiplying the radius times itself and then multiplying that product by π .		



Lesson 18: Date: More Problems on Area and Circumference 3/19/14







The area between the two quarter circles is $224ft^2 - 77ft^2 = 147 ft^2$.

Closing (5 minutes)

- The area of a semicircular region is $\frac{1}{2}$ of the area of a circle with the same radius.
- The area of a quarter of a circular region is $\frac{1}{4}$ of the area of a circle with the same radius.
- If a problem asks you to use $\frac{22}{7}$ for π , look for ways to use fraction arithmetic to simplify your computations in the problem.
- Problems that involve the composition of several shapes may be decomposed in more than one way.

Exit Ticket (5 minutes)





Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License.



This work is licensed under a

Name _____

Date_____

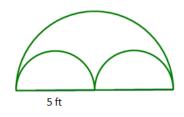
Lesson 18: More Problems on Area and Circumference

Exit Ticket

1. Ken's landscape gardening business creates odd shaped lawns which include semicircles. Find the area of this semicircular section of the lawn in this design. Use $\frac{22}{7}$ for π .



2. In the figure below, Ken's company has placed sprinkler heads at the center of the two small semicircles. The radius of the sprinklers is 5 ft. If the area in the larger semicircular area is the shape of the entire lawn, how much of the lawn will not be watered? Give your answer in terms of π and to the nearest tenth. Explain your thinking.





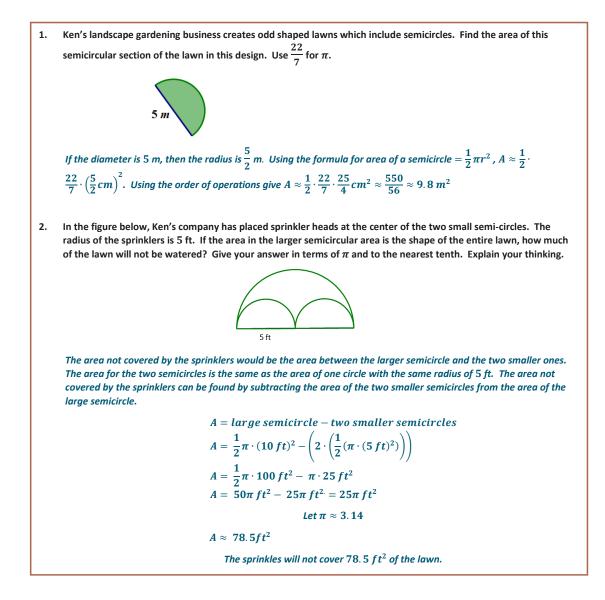
Lesson 18: Date: More Problems on Area and Circumference 3/19/14







Exit Ticket Sample Solutions





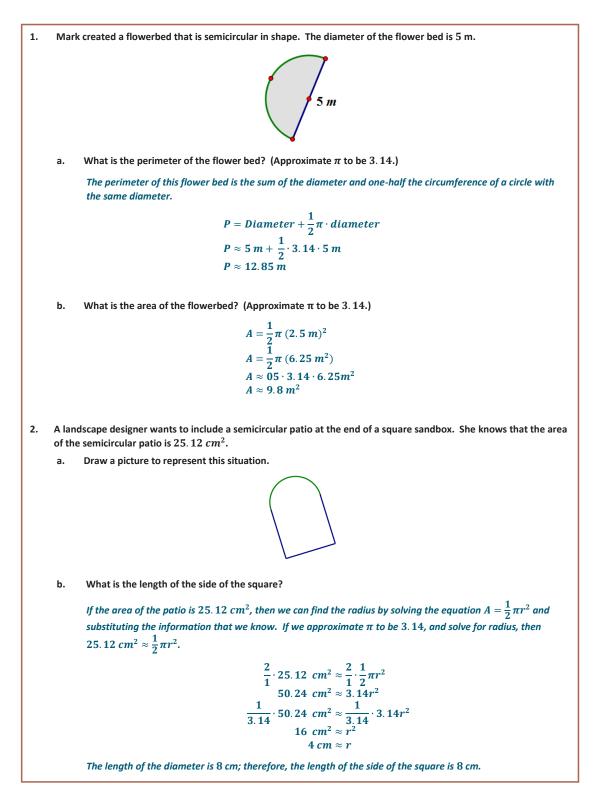
Lesson 18: Date: More Problems on Area and Circumference 3/19/14







Problem Set Sample Solutions

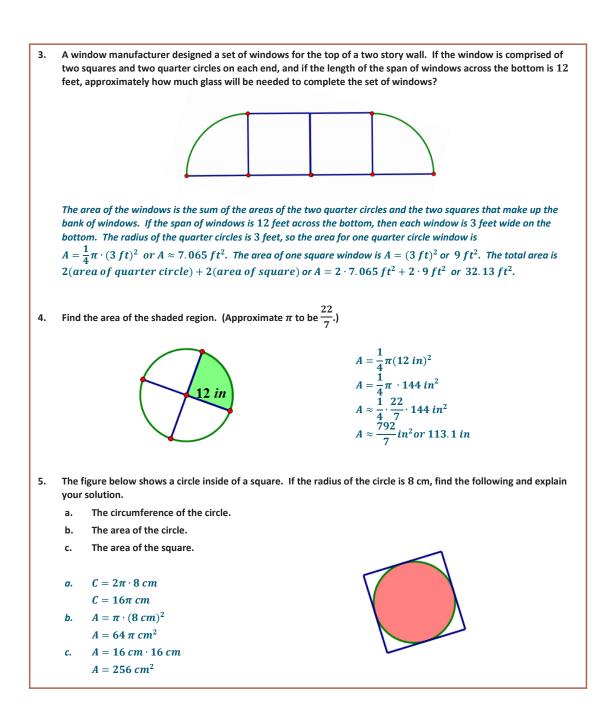




Lesson 18: Date: More Problems on Area and Circumference 3/19/14





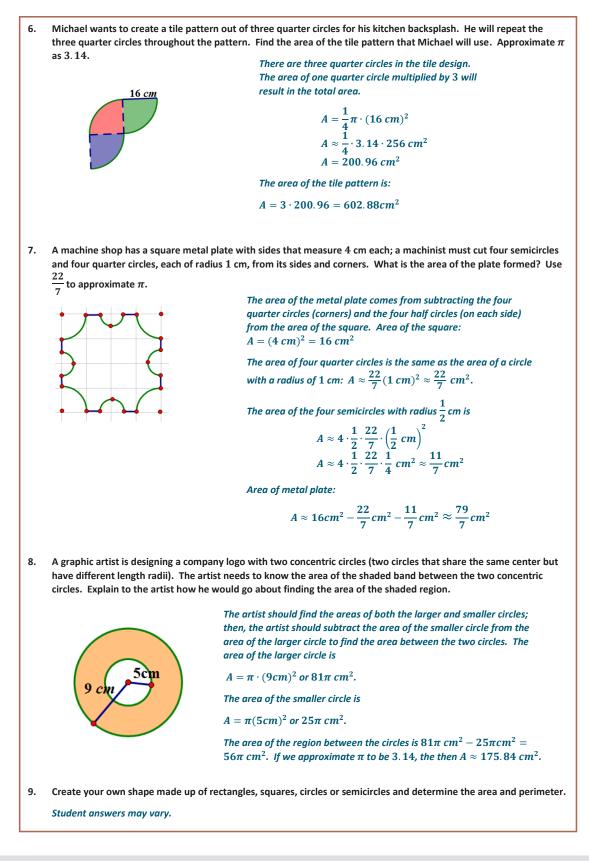




Lesson 18: Date: More Problems on Area and Circumference 3/19/14









Lesson 18: Date:

More Problems on Area and Circumference 3/19/14





This work is licensed under a Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License.