

# Lesson 15: Graphing Solutions to Inequalities

#### **Student Outcomes**

• Students graph solutions to inequalities taking care to interpret the solutions in the context of the problem.

Related Topics: More Lesson Plans for Grade 7 Common Core Math

#### Classwork

### **Opening Exercise (10 minutes)**

Students complete a two round sprint exercise where they practice their knowledge of solving linear inequalities in the form px + q > r and p(x + q) > r. Provide one minute for each round of the sprint. Follow the established protocol for a sprint exercise. Be sure to provide any answers not completed by students.



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## Sprint – Round 1

Write the solution of each inequality.

1. $x + 1 > 8$	23. $-\frac{1}{5}x > 2$
2. $x + 2 > 8$	24. $-\frac{2}{5}x > 2$
3. $x + 3 > 8$	25. $-\frac{3}{5}x > 3$
4. $x + 4 > 8$	26. $-\frac{4}{5}x > 4$
5. $x - 1 > 3$	27. $2x + 4 > 8$
6. $x - 2 > 3$	28. $2x + 5 > 9$
7. $x - 3 > 3$	29. $2x + 6 > 10$
8. $x - 4 > 3$	30. $2x - 1 < 5$
9. $3x > 15$	31. $2x - 3 < 5$
10. $3x > 18$	32. $2x - 5 < 5$
11. $3x > 21$	33. $-2x + 1 > 7$
12. $3x > 24$	34. $-2x + 2 > -8$
13. $-x > 4$	35. $-2x + 3 > 9$
14. $-x > 5$	36. $-3x + 1 > -8$
15. $-x > 6$	37. $-3x + 1 > 10$
16. $-x < -4$	38. $-3x + 1 > 13$
17. $-x < -5$	39. $2(x+3) > 4$
18. $-x < -6$	40. $3(x+3) < 6$
19. $\frac{1}{2}x > 1$	41. $4(x+3) > 8$
20. $\frac{1}{2}x > 2$	42. $-5(x-3) < -10$
21. $\frac{1}{2}x > 3$	43. $-2(x-3) > 8$
22. $\frac{1}{2}x > 4$	44. $-2(x+3) < 8$



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1 Answer Key			
1. $x + 1 > 8$	<i>x</i> > 7	$23.  -\frac{1}{5}x > 2$	<i>x</i> < -10
2. $x+2 > 8$	<i>x</i> > 6	$24.  -\frac{2}{5}x > 2$	<i>x</i> < -5
3. $x + 3 > 8$	<i>x</i> > 5	<b>25.</b> $-\frac{3}{5}x > 3$	<i>x</i> < -5
4. $x + 4 > 8$	<i>x</i> > 4	$26.  -\frac{4}{5}x > 4$	<i>x</i> < -5
5. $x - 1 > 3$	<i>x</i> > 4	<b>27.</b> $2x + 4 > 8$	<i>x</i> > 2
6. $x-2 > 3$	<i>x</i> > 5	28. $2x + 5 > 9$	<i>x</i> > 2
7. $x - 3 > 3$	<i>x</i> > 6	<b>29.</b> $2x + 6 > 10$	<i>x</i> > 2
8. $x-4 > 3$	<i>x</i> > 7	<b>30.</b> $2x - 1 < 5$	<i>x</i> < 3
9. $3x > 15$	<i>x</i> > 5	<b>31.</b> $2x - 3 < 5$	<i>x</i> < 4
<b>10.</b> $3x > 18$	<i>x</i> > 6	<b>32.</b> $2x-5 < 5$	<i>x</i> < 5
11. $3x > 21$	<i>x</i> > 7	<b>33.</b> $-2x + 1 > 7$	<i>x</i> < -3
<b>12.</b> $3x > 24$	<i>x</i> > 8	34. $-2x+2 > -8$	<i>x</i> < 5
<b>13.</b> $-x > 4$	<i>x</i> < -4	<b>35.</b> $-2x + 3 > 9$	<i>x</i> < -3
14. $-x > 5$	<i>x</i> < -5	<b>36.</b> $-3x + 1 > -8$	<i>x</i> < 3
<b>15.</b> $-x > 6$	<i>x</i> < -6	<b>37.</b> $-3x + 1 > 10$	<i>x</i> < -3
<b>16.</b> $-x < -4$	<i>x</i> > 4	<b>38.</b> $-3x + 1 > 13$	<i>x</i> < -4
<b>17.</b> $-x < -5$	<i>x</i> > 5	<b>39.</b> $2(x+3) > 4$	<i>x</i> > -1
<b>18.</b> $-x < -6$	<i>x</i> > 6	40. $3(x+3) < 6$	<i>x</i> < -1
<b>19.</b> $\frac{1}{2}x > 1$	<i>x</i> > 2	41. $4(x+3) > 8$	<i>x</i> > -1
$20.  \frac{1}{2}x > 2$	<i>x</i> > 4	42. $-5(x-3) < -10$	<i>x</i> > 5
$21.  \frac{1}{2}x > 3$	<i>x</i> > 6	<b>43.</b> $-2(x-3) > 8$	<i>x</i> < -1
22. $\frac{1}{2}x > 4$	<i>x</i> > 8	44. $-2(x+3) < 8$	x > -7



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## Sprint – Round 2

Write the solution of each inequality.

1. $x + 6 < 9$	23. $-\frac{1}{6}x < 2$
2. $x + 5 < 9$	24. $-\frac{2}{6}x < 2$
3. $x + 4 < 9$	25. $-\frac{3}{6}x < 3$
4. $x + 3 < 9$	26. $-\frac{4}{6}x < 4$
5. $x - 3 < 5$	27. $3x + 3 < 6$
6. $x - 4 < 5$	28. $3x + 4 < 7$
7. $x - 5 < 5$	29. $3x + 5 < 8$
8. $x - 6 < 5$	30. $3x - 1 > 5$
9. $4x < 20$	31. $3x - 4 > 5$
10. $4x < 16$	32. $3x - 7 > 5$
11. 4 <i>x</i> < 12	33. $-3x + 1 < 7$
12. $4x < 8$	34. $-3x + 2 < -7$
13. $-x < 6$	35. $-3x + 3 < 9$
14. $-x < 5$	36. $-4x + 1 < -11$
15. $-x < 4$	37. $-4x + 1 < -7$
16. $-x < -8$	38. $-4x + 1 < -3$
17. $-x < -7$	39. $3(x+2) < 9$
18. $-x < -6$	40. $4(x+2) < 12$
19. $\frac{1}{5}x < 1$	41. $5(x+2) > 15$
20. $\frac{1}{5}x < 2$	42. $-2(x+1) < 4$
21. $\frac{1}{5}x < 3$	43. $-3(2x-1) < -9$
22. $\frac{1}{5}x < 4$	44. $-5(4x+1) < 15$



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Round 2 Answer Key			
<b>1.</b> $x + 6 < 9$	<i>x</i> < 3	$23.  -\frac{1}{6}x < 2$	x > -12
2. $x + 5 < 9$	<i>x</i> < 4	24. $-\frac{2}{6}x < 2$	x > -6
3. $x + 4 < 9$	<i>x</i> < 5	<b>25.</b> $-\frac{3}{6}x < 3$	x > -6
4. $x + 3 < 9$	<i>x</i> < 6	$26.  -\frac{4}{6}x < 4$	x > -6
5. $x-3 < 5$	<i>x</i> < 8	27. $3x + 3 < 6$	<i>x</i> < 1
6. $x-4 < 5$	<i>x</i> < 9	<b>28.</b> $3x + 4 < 7$	<i>x</i> < 1
7. $x-5 < 5$	<i>x</i> < 10	<b>29.</b> $3x + 5 < 8$	<i>x</i> < 1
8. $x-6 < 5$	<i>x</i> < 11	<b>30.</b> $3x - 1 > 5$	<i>x</i> > 2
9. $4x < 20$	<i>x</i> < 5	31. $3x - 4 > 5$	<i>x</i> > 3
<b>10.</b> $4x < 16$	<i>x</i> < 4	32. $3x - 7 > 5$	<i>x</i> > 4
<b>11.</b> $4x < 12$	<i>x</i> < 3	<b>33.</b> $-3x + 1 < 7$	x > -2
<b>12.</b> $4x < 8$	<i>x</i> < 2	<b>34.</b> $-3x + 2 < -7$	<i>x</i> > 3
<b>13.</b> $-x < 6$	x > -6	<b>35.</b> $-3x + 3 < 9$	x > -2
14. $-x < 5$	x > -5	<b>36.</b> $-4x + 1 < -11$	<i>x</i> > 3
<b>15.</b> $-x < 4$	x > -4	<b>37.</b> $-4x + 1 < -7$	<i>x</i> > 2
<b>16.</b> $-x < -8$	<i>x</i> > 8	<b>38.</b> $-4x + 1 < -3$	<i>x</i> > 1
<b>17.</b> $-x < -7$	<i>x</i> > 7	<b>39.</b> $3(x+2) < 9$	<i>x</i> < 1
<b>18.</b> $-x < -6$	<i>x</i> > 6	<b>40.</b> $4(x+2) < 12$	<i>x</i> < 1
<b>19.</b> $\frac{1}{5}x < 1$	<i>x</i> < 5	41. $5(x+2) > 15$	<i>x</i> > 1
<b>20.</b> $\frac{1}{5}x < 2$	<i>x</i> < 10	<b>42.</b> $-2(x+1) < 4$	x > -3
<b>21.</b> $\frac{1}{5}x < 3$	<i>x</i> < 15	<b>43.</b> $-3(2x-1) < -9$	<i>x</i> > 2
$\boxed{22.  \frac{1}{5}x < 4}$	<i>x</i> < 20	44. $-5(4x+1) < 15$	x > -1

## Discussion

## Exercise 1 (10 minutes)

#### Exercise 1

1. Two identical cars need to fit into a small garage. The opening is 23 feet 6 inches wide, and there must be at least 3 feet 6 inches of clearance between the cars and between the edges of the garage. How wide can the cars be?



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Encourage students to begin by drawing a diagram to illustrate the problem. A sample diagram can be:



Have students try to find all of the widths that the cars could be. Challenge them to name one more width than the person next to them. While they name the widths, plot the widths on a number line at the front of the class to demonstrate the shading. Before plotting the widths, ask if the circle should be open or closed as a quick review of graphing inequalities. Ultimately, the graph should be



- Describe how to find the width of each car.
  - To find the width of each car, I subtract the minimum amount of space needed on either side of each car and in between the cars from the total length. Altogether this amount of space needed was 3(3.5) = 10.5 ft. Then, I divided the result, 23.5 10.5 = 13 by 2 since there were 2 cars. The answer would be no more than  $\frac{13}{2} = 6.5$  ft.
- Did you take an algebraic approach to finding the width of each car or an arithmetic approach? Explain.
  - Answers will vary.
- If arithmetic was used, ask "If w is the width of one car, write an inequality that can be used to find all possible values of w."
  - $2w + 10.5 \le 23.5$
- Why is an inequality used instead of an equation?
  - Since the minimum amount of space between the cars and each side of the garage is at least 3 feet
     6 inches, which equals 3.5 ft, the space could be larger than 3 feet 6 inches. If so, then the width of the cars would be smaller. Since the width in between the cars and on the sides is not exactly 3 feet 6 inches, and it could be more, then there are many possible car widths. An inequality will give all possible car widths.



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- If an algebraic approach was used initially ask, "How is the work shown in solving the inequality similar to the arithmetic approach?"
  - The steps to solving the inequality are the same as in an arithmetic approach. First, determine the total minimum amount of space needed by multiplying 3 by 3.5. Then, subtract 10.5 from the total of 23.5 and divide by 2.
- What happens if the width of each car is less than 6.5 feet?
  - The amount of space between the cars and on either side of the car and garage is more then 3 feet 6 inches.
- What happens if the width of each car is exactly 6.5 feet?
  - The amount of space between the cars and on either side of the car and garage is exactly 3 feet 6 inches.
- What happens if the width of each car is more than 6.5 feet?
  - The amount of space between the cars and on either side of the car and garage is less than 3 feet 6 inches.
- How many possible car widths are there?
  - Any infinite number of possible widths.
- What assumption is being made?
  - The assumption that the width of the car is greater than 0 feet. The graph illustrates all possible values less than 6.5 feet, but in the context of the problem, we know that the width of the car must be greater than 0 feet.
- Since we have determined there is an infinite amount, how can we illustrate this on a number line?
  - By a graph with a closed circle on 6.5 and an arrow drawn to the left.
- What if 6.5 feet could not be a width but all other possible measures less than 6.5 can be a possible width, how would the graph be different?
  - The graph would have an open circle on 6.5 and an arrow drawn to the left.

## Example 1 (8 minutes)

#### Example 1

A local car dealership is trying to sell all of the cars that are on the lot. Currently, it has 525 cars on the lot, and the general manager estimates that they will consistently sell 50 cars per week. Estimate how many weeks it will take for the number of cars on the lot to be less than 75.

Write an inequality that can be used to find the number of w full weeks. Since w is the number of full or complete weeks, when w = 1 means at the end of week 1.

525 - 50w < 75



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- Explain why 50w was subtracted from 525, and why the inequality less than was used?
  - Subtraction was used because the cars are being sold. Therefore, the inventory is being reduced. The less inequality than was used because the question asked for the number of cars remaining to be less than 75.
- In one of the steps, the inequality was reversed. Why did this occur?
  - The inequality in the problem reversed because both sides were multiplied by a negative number.



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## Exercise 2 (8 minutes): Optional

Have students complete the exercise individually then compare answers with a partner.





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## Game or Additional Exercises (12 minutes)

Make copies of the puzzle below and cut the puzzle into 16 smaller squares. Mix up the pieces. Give each student a puzzle, and tell them to put the pieces together to form a  $4 \times 4$  square. When pieces are joined, the problem on one side must be attached to the answer on the other. All problems on the top, bottom, right, and left must line up to the correct graph of the solution. The puzzle, how it is given below, is the answer key.





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## Additional Exercises (in Lieu of the Game)

For each problem, write, solve, and graph the inequality, and interpret the solution within the context of the problem.





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## **Closing (3 minutes)**

- Why do we use rays when graphing the solutions of an inequality on a number line?
- When graphing the solution of an inequality on a number line, how do you determine what type of circle, open or closed, to use?
- When graphing the solution of an inequality on a number line, how do you determine the direction of the arrow?

## Exit Ticket (4 minutes)



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Name \_\_\_\_\_

Date\_\_\_\_\_

## **Lesson 15: Graphing Solutions to Inequalities**

## **Exit Ticket**

The junior-high art club sells candles for a fundraiser. The first week of the fundraiser the club sells 7 cases of candles. Each case contains 40 candles. The goal is to sell at least 13 cases. During the second week of the fundraiser, the club meets its goal. Write, solve, and graph an inequality that can be used to find the possible number of candles sold the second week.



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## **Exit Ticket Sample Solutions**

The junior-high art club sells candles for a fundraiser. The first week of the fundraiser the club sells 7 cases of candles. Each case contains 40 candles. The goal is to sell at least 13 cases. During the second week of the fundraiser, the club meets its goal. Write, solve, and graph an inequality that can be used to find the minimum number of candles sold the second week.

n: the number candles sold the second week

$$\frac{n}{40} + 7 \ge 13$$
$$\frac{n}{40} + 7 - 7 \ge 13 - \frac{n}{40} \ge 6$$

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$$(40)\left(\frac{n}{40}\right) \ge 6(40)$$
$$n > 240$$

The minimum number of candles sold the second week was 240 candles.



*n*: the number of cases of candles sold the second week

 $40n + 280 \ge 520$  $40n + 280 - 280 \ge 520 - 280$  $40n+0 \geq 240$ 

$$\left(\frac{1}{40}\right)(40n) \ge 240\left(\frac{1}{40}\right)$$
$$n \ge 6$$



The minimum number of cases sold the second week was 6. Since there are 40 candles in each case, the minimum number of candles sold the second week would be (40)(6) = 240.



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## **Problem Set Sample Solutions**



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The maximum number of weeks Sally can withdraw the weekly dog sitter fee is 11 weeks.



On a cruise ship, there are two options for an internet connection. The first option is a fee of \$5 plus an additional 4. 0.25 per minute. The second option 50 for an unlimited number of minutes. For how many minutes, m, is the first option cheaper than the second option? Graph the solution.

m: number of minutes of internet connection

$$5 + 0.25m < 50$$
  

$$5 + 0.25m - 5 < 50 - 5$$
  

$$0.25m + 0 < 45$$
  

$$\left(\frac{1}{0.25}\right)(0.25m) < \left(\frac{1}{0.25}\right)(45)$$
  

$$m < 180$$

If there are less than 180 minutes, or 3 hours, used on the internet, then the first option would be cheaper. If 180 minutes or more are planned, then the second option is more economical.



5. The length of a rectangle is 100 centimeters, and its perimeter is greater than 400 centimeters. Henry writes an inequality and graphs the solution below to find the width of the rectangle. Is he correct? If yes, write and solve the inequality to represent the problem and graph. If no, explain the error(s) Henry made.



Henry's graph is incorrect. The inequality should be 2(100) + 2w > 400. When you solve the inequality you get w > 100. The circle on the number 100 on the number line is correct; however, the circle should be an open circle since the perimeter is not equal to 400. Also, the arrow should be pointing in the opposite direction because the perimeter is greater than, which means the arrow points to the right. The given graph indicates an inequality of less than or equal to.

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