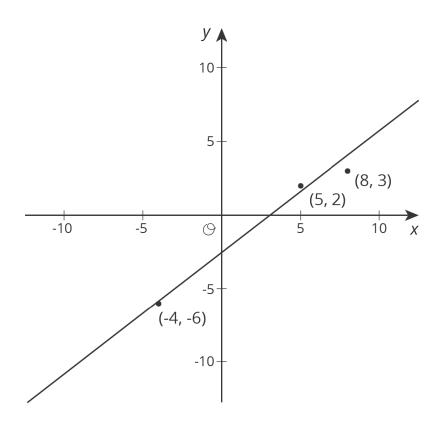


# Unit 6, Lesson 6: The Slope of a Fitted Line

Let's look at how changing one variable changes another.

### **6.1: Estimating Slope**

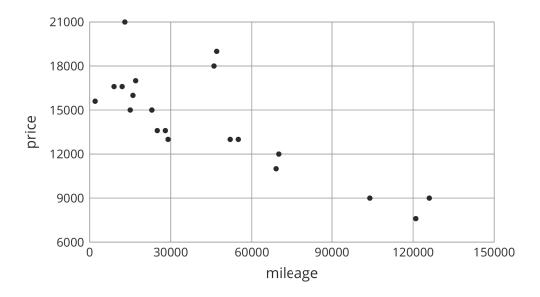
Estimate the slope of the line.

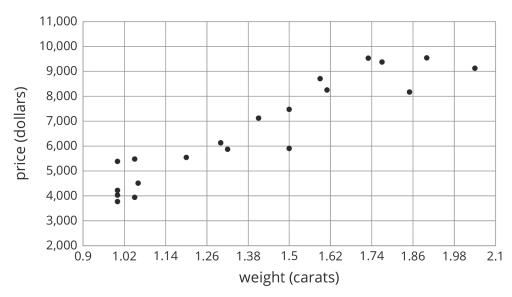


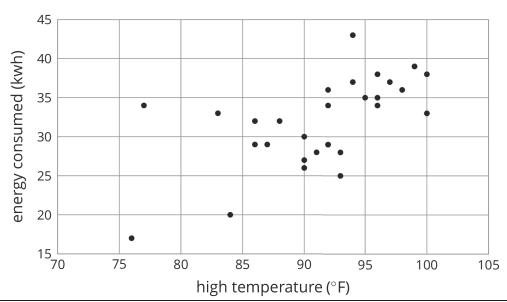
### **6.2: Describing Linear Associations**

For each scatter plot, decide if there is an association between the two variables, and describe the situation using one of these sentences:

- For these data, as \_\_\_\_\_\_ increases, \_\_\_\_\_ tends to increase.
- For these data, as \_\_\_\_\_\_ increases, \_\_\_\_\_ tends to decrease.
- For these data, \_\_\_\_\_ and \_\_\_\_ do not appear to be related.







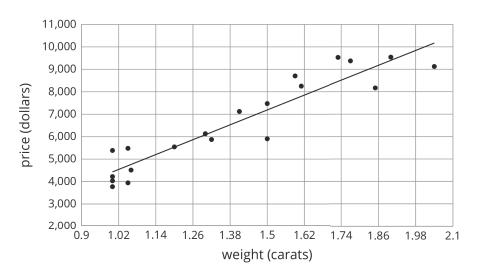


## **6.3: Interpreting Slopes**

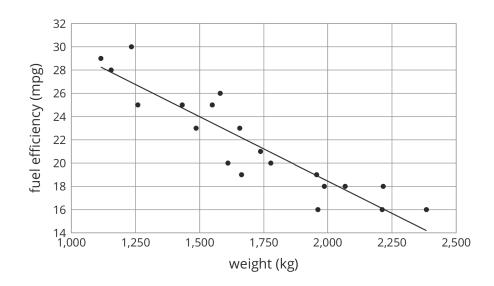
For each of the situations, a linear model for some data is shown.

- 1. What is the slope of the line in the scatter plot for each situation?
- 2. What is the meaning of the slope in that situation?

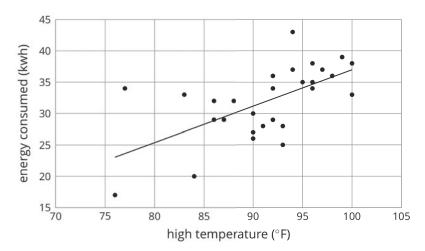
$$y = 5,520.619x - 1,091.393$$



$$y = -0.011x + 40.604$$

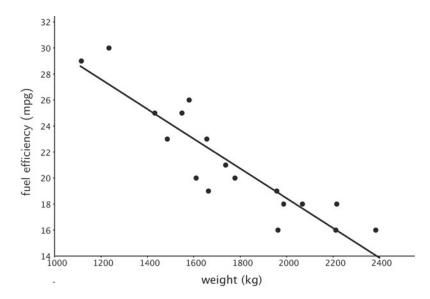


$$y = 0.59x - 21.912$$



#### Are you ready for more?

The scatter plot shows the weight and fuel efficiency data used in an earlier lesson along with a linear model represented by the equation y = -0.0114x + 41.3021.



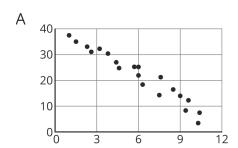
- 1. What is the value of the slope and what does it mean in this context?
- 2. What does the other number in the equation represent on the graph? What does it mean in context?

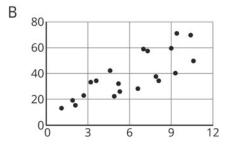


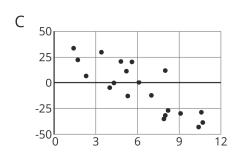
- 3. Use the equation to predict the fuel efficiency of a car that weighs 100 kilograms.
- 4. Use the equation to predict the weight of a car that has a fuel efficiency of 22 mpg.
- 5. Which of these two predictions probably fits reality better? Explain.

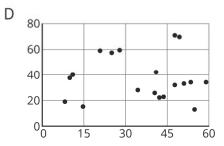
#### **6.4: Positive or Negative?**

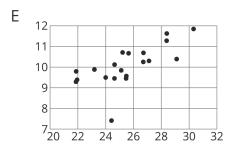
1. For each of the scatter plots, decide whether it makes sense to fit a linear model to the data. If it does, would the graph of the model have a positive slope, a negative slope, or a slope of zero?







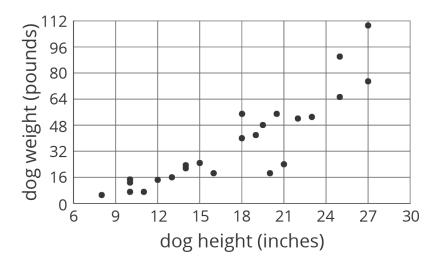




2. Which of these scatter plots show evidence of a positive association between the variables? Of a negative association? Which do not appear to show an association?

#### **Lesson 6 Summary**

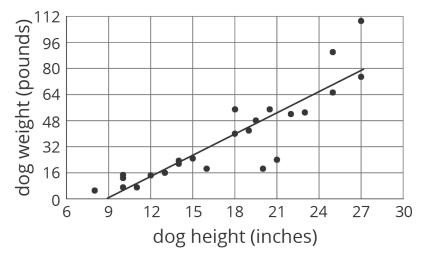
Here is a scatter plot that we have seen before. As noted earlier, we can see from the scatter plot that taller dogs tend to weigh more than shorter dogs. Another way to say it is that weight tends to increase as height increases. When we have a positive association between two variables, an increase in one means there tends to be an increase in the other.



We can quantify this tendency by fitting a line to the data and finding its slope. For example, the equation of the fitted line is

$$w = 4.27h - 37$$

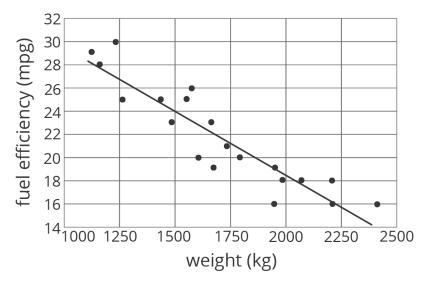
where h is the height of the dog and w is the predicted weight of the dog.



The slope is 4.27, which tells us that for every 1-inch increase in dog height, the weight is predicted to increase by 4.27 pounds.



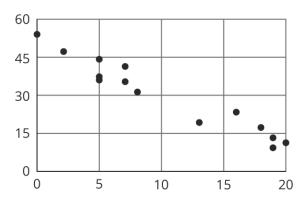
In our example of the fuel efficiency and weight of a car, the slope of the fitted line shown is -0.01.



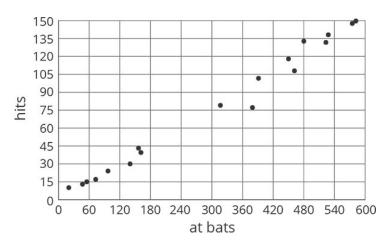
This tells us that for every 1-kilogram increase in the weight of the car, the fuel efficiency is predicted to decrease by 0.01 miles per gallon. When we have a negative association between two variables, an increase in one means there tends to be a decrease in the other.

## Unit 6, Lesson 6: The Slope of a Fitted Line

1. Which of these statements is true about the data in the scatter plot?



- A. As *x* increases, *y* tends to increase.
- B. As *x* increases, *y* tends to decrease.
- C. As *x* increases, *y* tends to stay unchanged.
- D. *x* and *y* are unrelated.
- 2. Here is a scatter plot that compares hits to at bats for players on a baseball team.

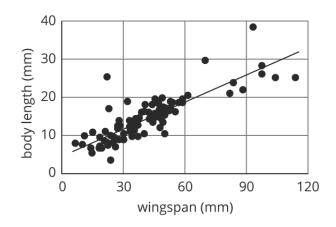


Describe the relationship between the number of at bats and the number of hits using the data in the scatter plot.

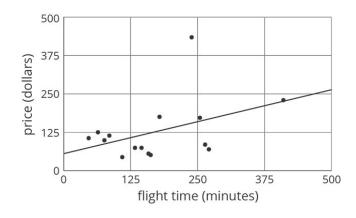
3. The linear model for some butterfly data is given by the equation y = 0.238x + 4.642. Which of the following best describes the slope of the model?







- A. For every 1 mm the wingspan increases, the length of the butterfly increases 0.238 mm.
- B. For every 1 mm the wingspan increases, the length of the butterfly increases 4.642 mm.
- C. For every 1 mm the length of the butterfly increases, the wingspan increases 0.238 mm.
- D. For every 1 mm the length of the butterfly increases, the wingspan increases 4.642 mm.
- 4. Nonstop, one-way flight times from O'Hare Airport in Chicago and prices of a one-way ticket are shown in the scatter plot.



- a. Circle any data that appear to be outliers.
- b. Use the graph to estimate the difference between any outliers and their predicted values.

(from Unit 6, Lesson 4)

5. Solve: 
$$\begin{cases} y = -3x + 13 \\ y = -2x + 1 \end{cases}$$

(from Unit 4, Lesson 14)