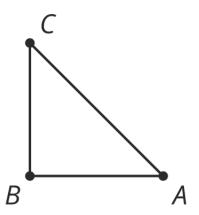


Unit 1, Lesson 8: Rotation Patterns

Let's rotate figures in a plane.

8.1: Building a Quadrilateral

Here is a right isosceles triangle:



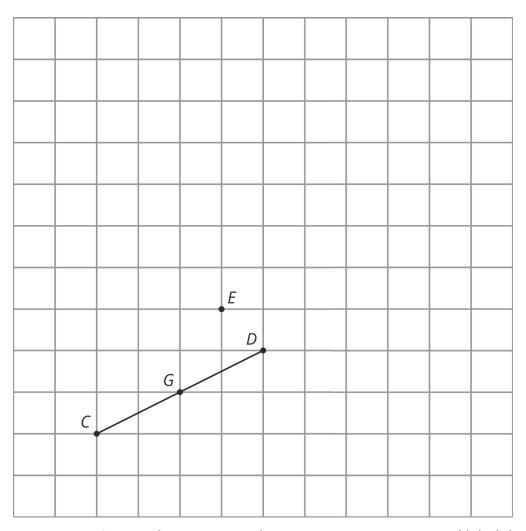
- 1. Rotate triangle *ABC* 90 degrees clockwise around *B*.
- 2. Rotate triangle *ABC* 180 degrees clockwise round *B*.
- 3. Rotate triangle *ABC* 270 degrees clockwise around *B*.
- 4. What would it look like when you rotate the four triangles 90 degrees clockwise around *B*? 180 degrees? 270 degrees clockwise?



8.2: Rotating a Segment

m.openup.org/1/8-1-8-2

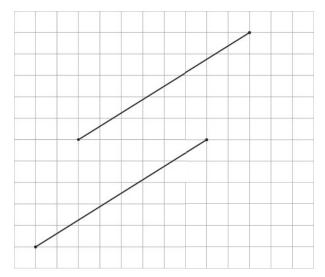




- 1. Rotate segment CD 180 degrees around point D. Draw its image and label the image of C as A.
- 2. Rotate segment CD 180 degrees around point E. Draw its image and label the image of C as B and the image of D as F.
- 3. Rotate segment ${\it CD}$ 180 degrees around its midpoint, ${\it G}$. What is the image of ${\it C}$?
- 4. What happens when you rotate a segment 180 degrees around a point?

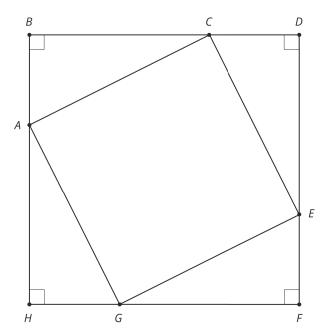


Are you ready for more?



Here are two line segments. Is it possible to rotate one line segment to the other? If so, find the center of such a rotation. If not, explain why not.

8.3: A Pattern of Four Triangles



m.openup.org/1/8-1-8-3



You can use rigid transformations of a figure to make patterns. Here is a diagram built with three different transformations of triangle *ABC*.

1. Describe a rigid transformation that takes triangle *ABC* to triangle *CDE*.

2. Describe a rigid transformation that takes triangle ABC to triangle EFG.

3. Describe a rigid transformation that takes triangle *ABC* to triangle *GHA*.

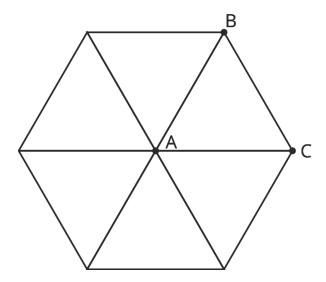
4. Do segments AC, CE, EG, and GA all have the same length? Explain your reasoning.

Lesson 8 Summary

When we apply a 180-degree rotation to a line segment, there are several possible outcomes:

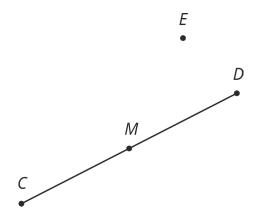
- The segment maps to itself (if the center of rotation is the midpoint of the segment).
- The image of the segment overlaps with the segment and lies on the same line (if the center of rotation is a point on the segment).
- The image of the segment does not overlap with the segment (if the center of rotation is *not* on the segment).

We can also build patterns by rotating a shape. For example, triangle ABC shown here has $m(\angle A) = 60$. If we rotate triangle ABC 60 degrees, 120 degrees, 180 degrees, 240 degrees, and 300 degrees clockwise, we can build a hexagon.



Unit 1, Lesson 8: Rotation Patterns

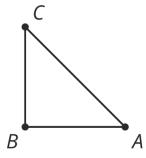
1. For the figure shown here,



- a. Rotate segment CD 180° around point D.
- b. Rotate segment CD 180° around point E.
- c. Rotate segment CD 180° around point M.
- 2. Here is an isosceles right triangle:

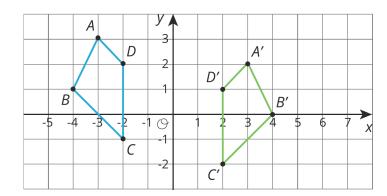
Draw these three rotations of triangle *ABC* together.

- a. Rotate triangle ABC 90 degrees clockwise around A.
- b. Rotate triangle ABC 180 degrees around A.
- c. Rotate triangle ABC 270 degrees clockwise around A.

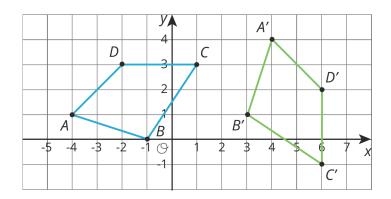


3. Each graph shows two polygons ABCD and A'B'C'D'. In each case, describe a sequence of transformations that takes ABCD to A'B'C'D'.

a.

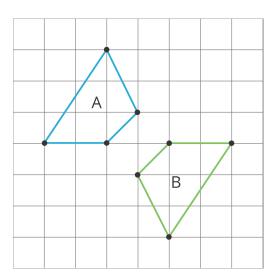


b.



(from Unit 1, Lesson 5)

4. Lin says that she can map Polygon A to Polygon B using *only* reflections. Do you agree with Lin? Explain your reasoning.



(from Unit 1, Lesson 4)